I am going to explain some, largely conjectural, connections between birational geometry and derived categories of coherent sheaves. I will present joint work with David Ploog and Pawel Sosna which is a contribution towards some of the popular conjectures in the set-up of cyclic quotient singularities.