I will present the following result obtained in a recent joint work with Yongnam Lee.
Theorem: Let $K$ be the function field of a very general complex surface of degree $d>4$ in the projective 3dimensional space. Let $L$ be a proper subfield of $K$ that contains properly the base field $C$. Then $L$ is isomorphic either to $C(x)$, if the transcendental degree of $L$ is 1 , or to $C(x, y)$ if $L$ has transcendental degree 2. Similar results hold for the very general product of two curves.

