Orlov's famous representability theorem asserts that any fully faithful exact functor between the bounded derived categories of coherent sheaves on smooth projective varieties is a Fourier-Mukai functor. We will show that this result is false without the fully faithfulness hypothesis. This is joint work with Michel Van den Bergh.