

I will describe the basics of symplectic and Poisson geometry on derived moduli spaces, including the main existence theorems, and explain briefly how one can obtain a quantization of the derived category of quasi-coherent Modules on a moduli space equipped with a Poisson structure.