

Motivated by the relation between (twisted) K3 surfaces and special cubic fourfolds, we construct moduli spaces of polarized twisted K3 surfaces of any fixed degree and order. We do this by mimicking the construction of the moduli of untwisted K3 surfaces as a quotient of a bounded symmetric domain. We discuss a possible arithmetic application, as suggested by A. Várilly-Alvarado.