

Let M be the moduli space of stable curves of genus g . The aim of this talk is to describe many new modular compactifications of the moduli space of smooth curves, which are related to the minimal model program of M .
This is a joint work in progress with Giulio Codogni and Filippo Viviani.