

It is a classical Theorem that moduli spaces of sheaves on a projective K3 surface are Hyperkähler varieties of expected dimension, deformation equivalent to the Hilbert scheme of points on a K3 surface. In this talk I will describe a new proof of this result that uses Bridgeland stability conditions in families and wall-crossing to construct the deformation equivalence.