Motivic homotopy theory arose in the 1990s as a way of doing homotopy theory for algebraic varieties. Since then, it has developed into a generalization of classical homotopy theory with active developments in its own right and a powerful tool for understanding arithmetic aspects in algebra. This talk discusses Milnor's conjecture from the 1970s relating Galois cohomology to quadratic forms.