

A famous theorem by Siu states that plurigenera are invariant under smooth deformations for complex projective manifolds, a result which is a cornerstone of higher dimensional moduli theory. In this talk we will explore some examples showing that Siu's theorem fails in positive and mixed characteristic, then discuss the implications at the level of moduli theory, as well as some related questions.