

In this talk I will survey some recent results about sheaves on hyper-Kähler manifolds that behave like sheaves on K3 surfaces. I will present a result obtained jointly with F. Meazzini and I will discuss some open problems.