Over the complex numbers, the moduli space of principally polarised abelian g-folds is unirational if and only if g<6. We consider questions about the near-rationality of these spaces over the rational numbers, and some related arithmetic questions about the existence of lifts of abelian varieties over F_p to the rational numbers. This is joint work with Daniel Loughran.