Motivated by finding locally complete projective families of generalized Kummer fourfolds, we study projective duality for some projective models of generalized Kummer fourfolds. This is based on joint work in progress with D. Agostini, P. Beri, and Á.D. Ríos-Ortiz.