We will present some recent results and some open conjectures relating holomorphic differentials and the fundamental group of a compact Kaehler manifold, then we will apply some elementary constructions on semiample vector bundles to partially answer some of these open questions.