In recent work by Arena, Canning, Clader, Haburcak, Li, Mok and Tamborini, it was proven that, for infinitely many values of g and n, non-tautological algebraic cohomology classes exist on the moduli space Mg,n of smooth, genus g, n-pointed curves. In this talk, we will describe how a small generalization of their technique can be used to cover most of the remaining cases, thereby proving the existence of non-tautological algebraic cohomology classes on the Mg,n moduli space for all but a finite number of values of g and n.