

Esercizio 1

$$(x_i, y_i) = (0 \text{ m}, 0 \text{ m})$$

$$x_f = 130 \text{ m}$$

$$y_f = 20.0 \text{ m}$$

$$x_f = x_i + v_{xi} t = v_i t \cos 35.0^\circ$$

$$v_i t \cos 35.0^\circ = 130 \text{ m} \Rightarrow v_i t = 158.7 \text{ m}$$

$$y_f = v_{yi} t - \frac{1}{2} g t^2$$

$$y_f = (v_i \sin 35.0^\circ) t - \frac{1}{2} \cdot (9.80 \text{ m/s}^2) \cdot t^2$$

(usando  $v_i t = 158.7 \text{ m}$ )

$$\Rightarrow t = \sqrt{\frac{71.0 \text{ m}}{4.90 \text{ m/s}^2}} = 3.81 \text{ s} \quad (b)$$

$$v_i = 41.7 \text{ m/s} \quad (a)$$

*de*



Esercizio 2

$$h = 6 \text{ m}$$

$$r = 2 \text{ m}$$

$$m g h = \frac{1}{2} m v_f^2 + m g e r$$

$$v_f = \sqrt{2g(h - 2r)} = \sqrt{2g(r)} \quad (h = 3r)$$

$$a = \frac{v_f^2}{r} = \frac{2g}{2} = 19.6 \text{ m/s}^2$$

$$m \frac{v_f^2}{r} = m g + N$$

$$N = \frac{2m g (h - 2r)}{r} - m g = m g \left( \frac{2h}{r} - 5 \right)$$

$$h = 3r$$

$$N = \frac{2m}{r} (g \cdot 3r - 2r g) = 2m g \left( \frac{3r}{r} - 2 \right) = 2m g (3 - 2) = 2m g$$

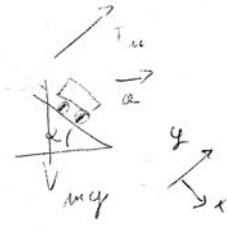
$$= \frac{2m}{r} \cdot g \cdot r = 2m g = 9.8 \text{ N}$$

N° 2

$$m g \left( \frac{2h}{r} - 4 - 1 \right) = m g \left( \frac{2h}{r} - 5 \right) =$$

$$= 1.9.8 \cdot \left( \frac{2 \cdot 6}{2} - 5 \right) = 9.8 \cdot 1 = 9.8 \text{ N}$$

### Esercizio 3



$$\frac{mv^2 \cos \alpha}{R} = mg \sin \alpha$$

$$R = 200 \text{ m}$$

$$v = 50 \text{ km/h}$$

$$\begin{cases} x & N \sin \alpha = m \frac{v^2}{R} \\ y & N \cos \alpha = mg \end{cases}$$

$$\frac{\sin \alpha}{\cos \alpha} = \frac{v^2}{gR}$$

$$\alpha = \arctan \frac{v^2}{gR} = \frac{(50 \times 10^3 / 3600)^2}{9.8 \cdot 200} = 23.26^\circ$$

5.6°

### Esercizio 4

$$\theta(t) = A \cos \omega t$$

$$v_{\max} = \frac{d\theta}{dt} = A\omega = 0.073 \text{ rad/s}$$

$$\Rightarrow \left( \omega = \sqrt{\frac{g}{L}} = 0.52 \text{ Hz} \right)$$

$$A = 0.14 \text{ rad}$$

$$T = \frac{2\pi}{\omega} = 12.08 \text{ s}$$

$$a_{\max} = A\omega^2 = 0.14 \cdot (0.52)^2 \frac{\text{rad}}{\text{s}^2} = 0.038 \frac{\text{rad}}{\text{s}^2}$$

$$N = 26000 \text{ km/h}$$

Exercise 5

$$a) \quad F = \frac{GM_T M_T}{r^2} = \frac{M_T^2 N^2}{r^2}$$

$$r = \frac{GM_T}{N^2} = \frac{6.67 \times 10^{-11} \cdot 5.98 \times 10^{24}}{(26000 \times 10^3 / 3600)^2}$$

$$= 7.65 \times 10^6 \text{ m}$$

$$h = r - R_T = 7.65 \times 10^6 - 6.38 \times 10^6 = 1.267 \times 10^6 \text{ m}$$

$$b) \quad T = \frac{2\pi}{\omega} \quad \omega = \frac{N}{r} = 0.0010^{-1}$$

$$= 1.74 \text{ h. (6652 s)}$$

$$c) \quad G m_{\text{net}} M$$